



National 5 Maths Quadratic Graphs

SQA past paper and specimen paper
questions and answers by topic

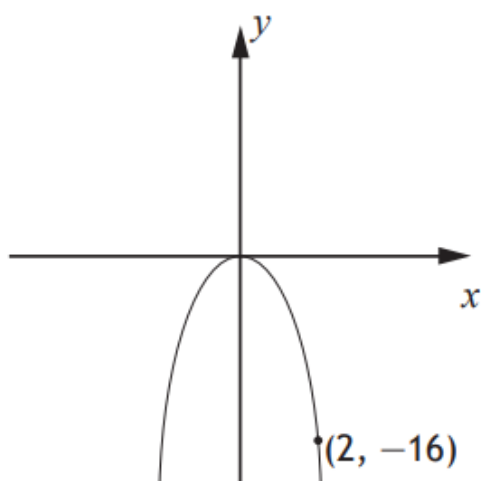
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The graph with equation $y = kx^2$ is shown below.



The point $(2, -16)$ lies on the graph.

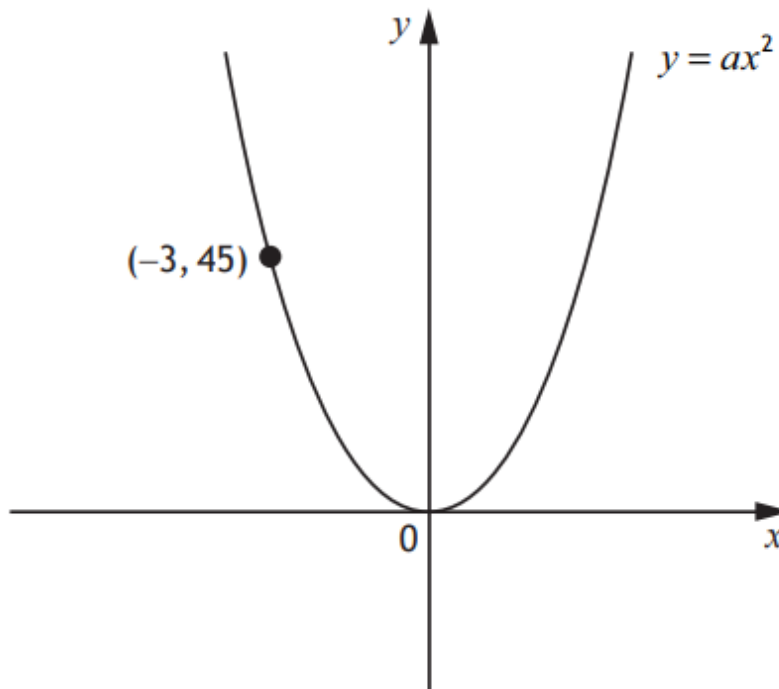
Determine the value of k .

2

Answer:

-4

The diagram below shows part of the graph of $y = ax^2$



Find the value of a .

2

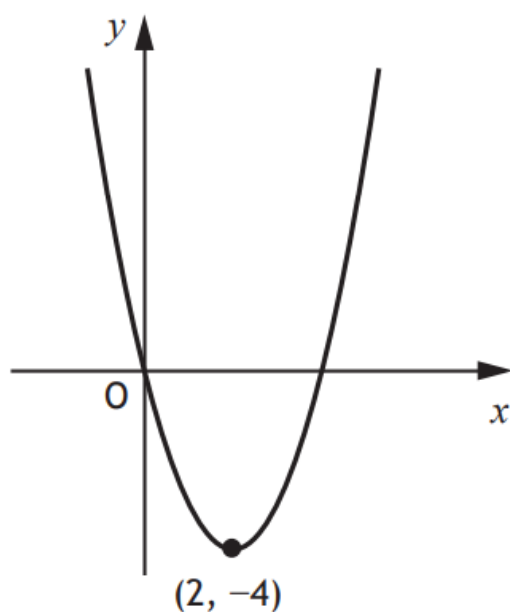
Answer:

$$a = 5$$



The graph below shows part of the parabola with equation of the form

$$y = (x + a)^2 + b.$$



The minimum turning point $(2, -4)$ is shown in the diagram.

(a) State the values of

(i) a 1

(ii) b . 1

(b) Write down the equation of the axis of symmetry of the graph. 1

Answers:

(a) (i) $a = -2$

(ii) $b = -4$

(b) $x = 2$

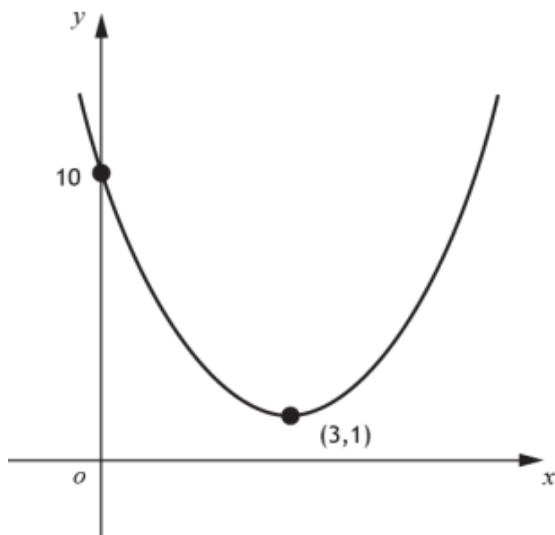
National 5 Maths
SQA 2016 Paper 1
Question 10

Sketch the graph of $y = (x - 3)^2 + 1$.

On your sketch, show clearly the coordinates of the turning point and the point of intersection with the y -axis.

3

Answer:



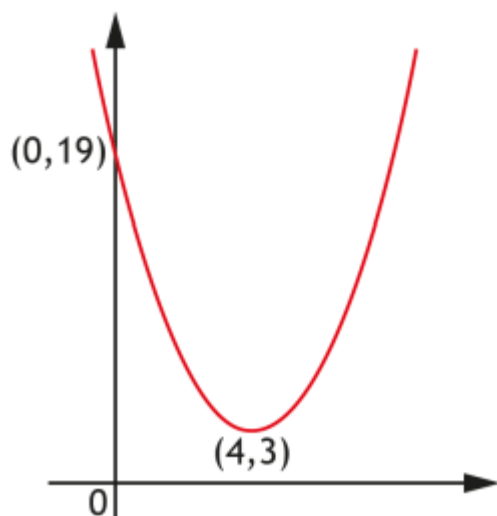
A parabola has equation $y = x^2 - 8x + 19$.

- (a) Write the equation in the form $y = (x - p)^2 + q$. 2
- (b) Sketch the graph of $y = x^2 - 8x + 19$, showing the coordinates of the turning point and the point of intersection with the y -axis. 3

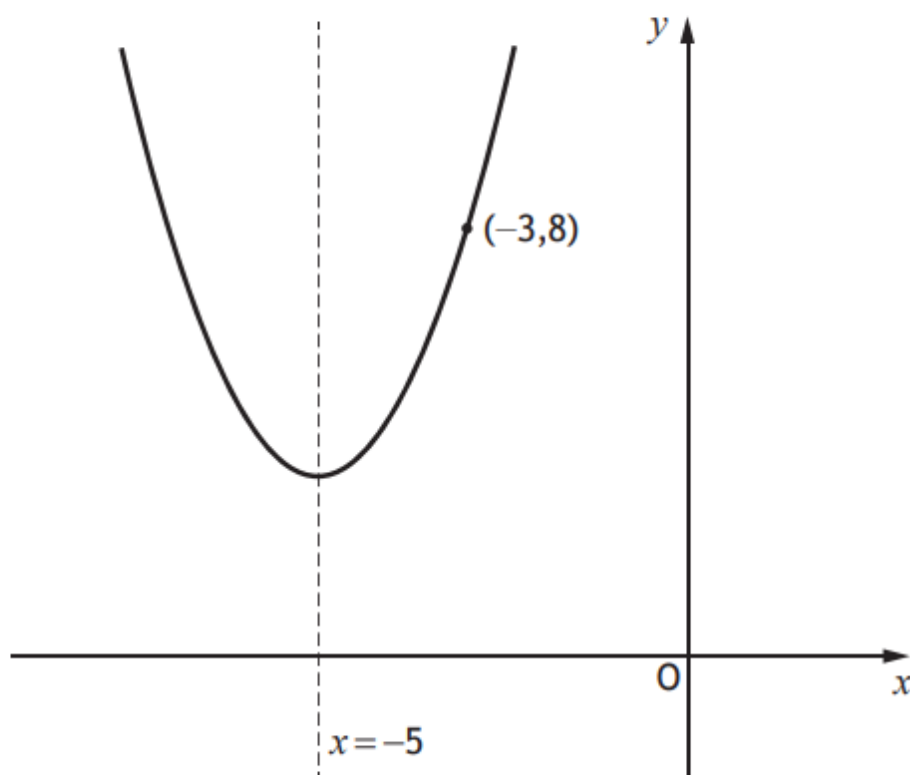
Answers:

(a) $y = (x - 4)^2 + 3$

(b)



The graph below shows a parabola with equation of the form $y = (x + a)^2 + b$.



The equation of the axis of symmetry of the parabola is $x = -5$.

(a) State the value of a . 1

The point $(-3, 8)$ lies on the parabola.

(b) Calculate the value of b . 2

Answers:

(a) $a = 5$

(b) $b = 4$

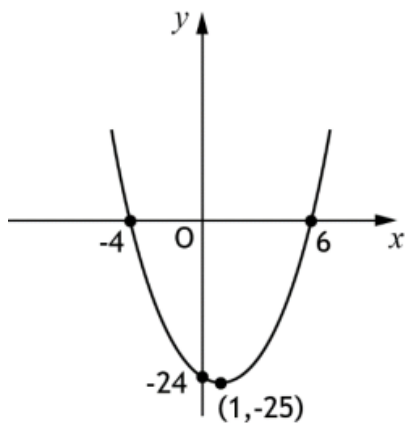
National 5 Maths
SQA 2018 Paper 1
Question 16

Sketch the graph of $y = (x - 6)(x + 4)$.

On your sketch, show clearly the points of intersection with the x -axis and the y -axis, and the coordinates of the turning point.

3

Answer:





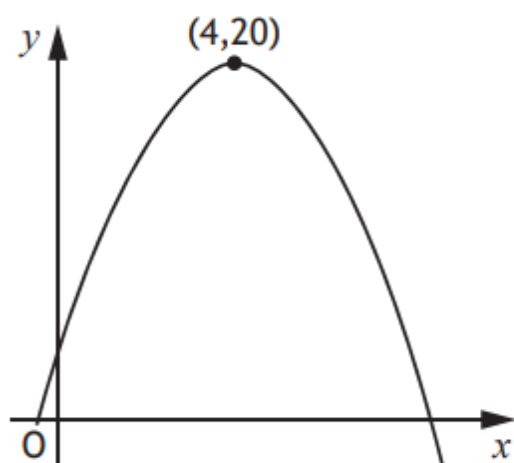
-
- (a) (i) Express $x^2 - 6x - 81$ in the form $(x - p)^2 + q$. 2
- (ii) Hence state the equation of the axis of symmetry of the graph of $y = x^2 - 6x - 81$. 1
- (b) The roots of the equation $x^2 - 6x - 81 = 0$ can be expressed in the form $x = d \pm d\sqrt{e}$.
Find, algebraically, the values of d and e . 4
-

Answer:

- (a) (i) $(x - 3)^2 - 90$
(ii) $x = 3$
- (b) $d = 3, e = 10$



The graph shows a parabola.



The maximum turning point has coordinates $(4, 20)$ as shown in the diagram.

(a) Write down the equation of the axis of symmetry of the graph. 1

The equation of the parabola is of the form $y = b - (x + a)^2$.

(b) State the values of

(i) a 1

(ii) b . 1

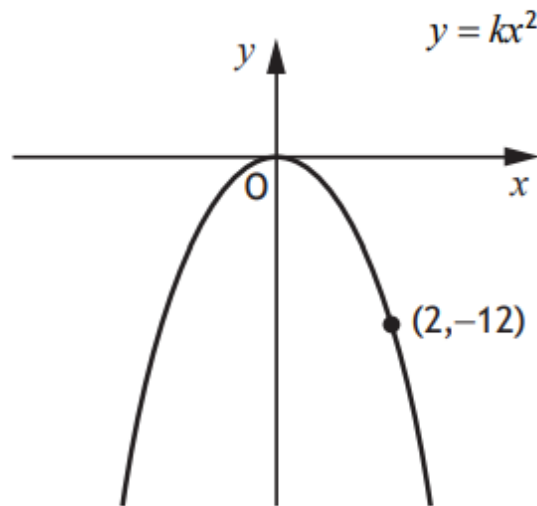
Answers:

(a) $x = 4$

(b) (i) -4

(ii) 20

The diagram below shows part of the graph of $y = kx^2$.



Find the value of k .

2

Answer:

-3

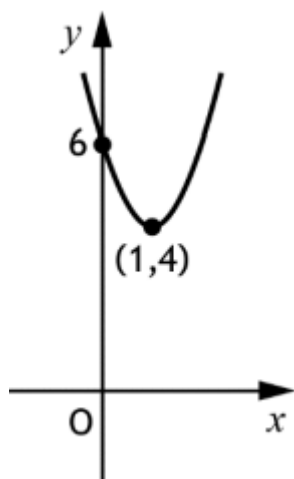
National 5 Maths
SQA 2021 Paper 1
Question 17

Sketch the graph of $y = 2(x-1)^2 + 4$.

On your sketch, show clearly the coordinates of the turning point and the point of intersection with the y -axis.

3

Answer:





(a) Express $x^2 + 8x + 15$ in the form $(x + a)^2 + b$. 2

(b) Hence, or otherwise, state the coordinates of the turning point of the graph of $f(x) = x^2 + 8x + 15$. 1

Answers:

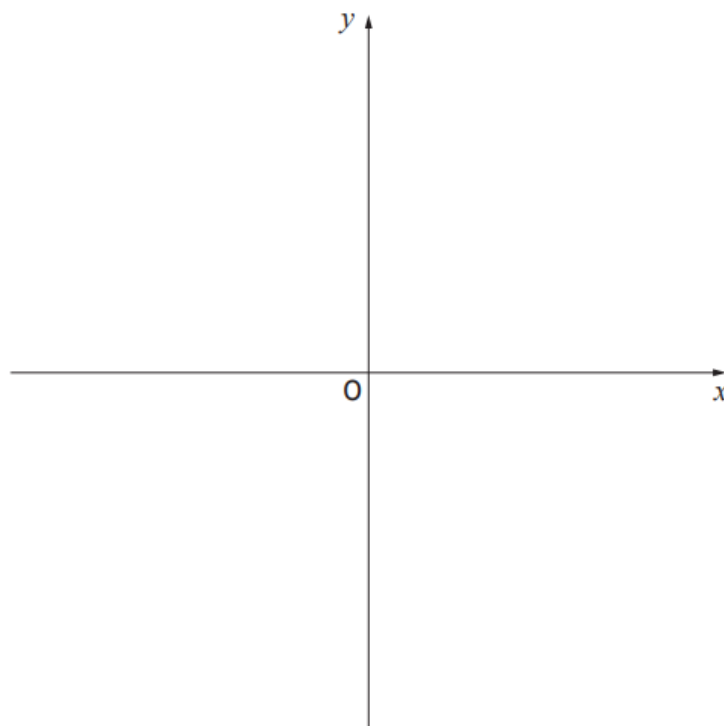
(a) $(x + 4)^2 - 1$

(b) $(-4, -1)$

Sketch the graph of $y = (x + 1)(x - 3)$ using the axes provided below.

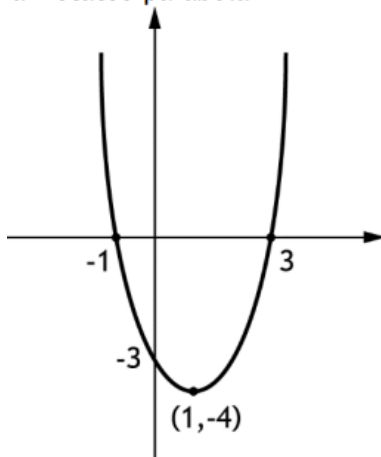
On your sketch, show clearly the points of intersection with the x -axis and the y -axis, and the coordinates of the turning point.

3

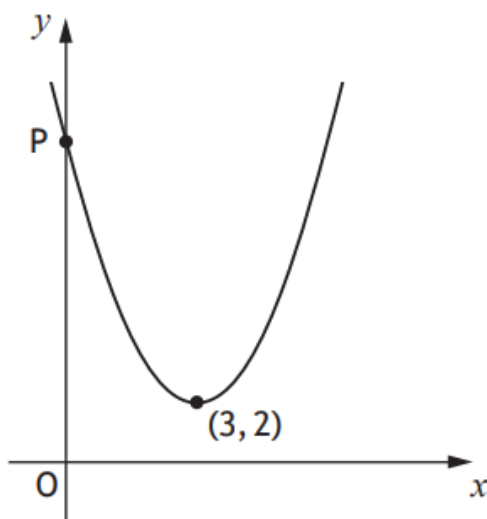


Answer:

$(1, -4)$ AND -3 and a consistently annotated parabola



The graph below shows part of a parabola of the form $y = (x + a)^2 + b$.



- (a) (i) State the value of a . 1
- (ii) State the value of b . 1
- (b) P is the point $(0, c)$.
Find the value of c . 1

Answers:

- (a) (i) -3
(ii) 2
- (b) 11

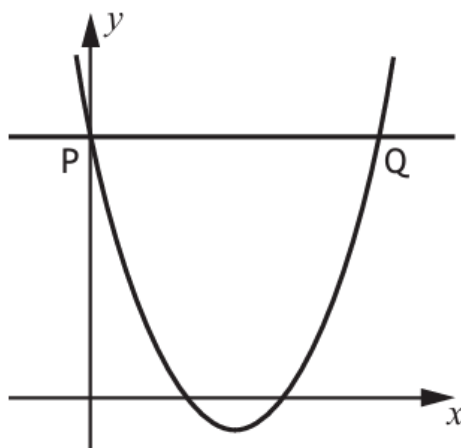
(a) Express $x^2 - 6x + 8$ in the form $(x - a)^2 + b$. 2

(b) Hence, or otherwise, state the coordinates of the turning point of the graph of $y = x^2 - 6x + 8$. 1

The diagram shows the graph of $y = x^2 - 6x + 8$.

A line PQ has been drawn parallel to the x -axis, where:

- P lies on the y -axis
- P and Q lie on the graph of $y = x^2 - 6x + 8$.



(c) Find the coordinates of Q. 2

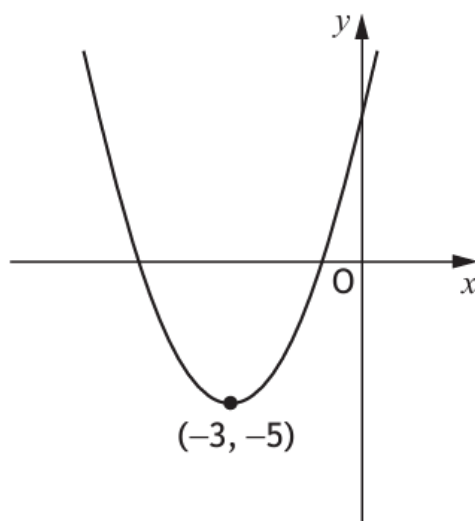
Answers:

(a) $(x - 3)^2 - 1$

(b) $(3, -1)$

(c) $(6, 8)$

The diagram shows a parabola with equation of the form $y = (x + a)^2 + b$.



- (a) State the value of a . 1
- (b) State the value of b . 1

Answers:

- (a) $a = 3$
- (b) $b = -5$